

ARE YOU READY FOR CALCULUS ?

Name _____

Complete the following problems on separate paper. Show work for each problem!

1. Completely factor: $4x^2 - 36$

2. If $x = 3$ and $y = 5$, and $\frac{1}{z} = \frac{1}{x} + \frac{1}{y}$, then $z = ?$

3. Simplify: $\frac{x^{-2}y^{-6}}{3x^{-4}y^3}$

4. Simplify: $\left(x^{\frac{1}{2}}x^{\frac{3}{4}}\right)^{\frac{1}{7}}$

5. Simplify: $(\sqrt{3x} + \sqrt{5x})^2$

6. Simplify: $3x^{\frac{-2}{3}} \cdot 4x^{\frac{1}{2}} =$

7. Simplify: $\sqrt[3]{24x^3y^{12}}$

8. Simplify: $\left(\frac{3x^2y^3}{xw^{-2}}\right)^3 =$

9. Evaluate: $\frac{1}{27^{\frac{-1}{3}}}$

10. Write in exponential form: $\sqrt[3]{7x^2y^6}$

11. Multiply: $(3x - 7)(2x + 9)$

12. Factor: $x^2 + x - 12$

13. If $y = \left(\frac{1}{2}\right)^x$, find y when $x = -2$.

14. Solve: $(3-x)(1+x) < 0$

15. If the two solutions of the quadratic equation $4x^2 + 4x + k = 0$ are equal, find "k" .

16. If the roots of a quadratic equation are $-3/2$ and $4/5$, find one possible equation.

17. The equation of the line containing the points $(1, 5)$ and $(4, 3)$ is :

18. Translate the following. Do not solve. C varies jointly as d and the cube of e, and inversely as the square root of m.

19. Determine if $(x + 2)$ is a factor of $x^5 + 3x^4 - 2x + 4$.

20. How many different real numbers satisfy the equation $6x - x^2 = 9$?

21. If $a^{10} = 4900$, find a^5 .

22. Write as a single log. $\log 6 + \log 5 - \log 3$

23. Change $\log_{10} 10,000 = 4$ to exponential.

24. Solve for b: $\log_b 81 = 4$.

25. Simplify: $\log_2 \left[\left(\sqrt[3]{x} \right) y \right]$

26. Sketch: $y = 1 + \log(x)$

27. Solve: $\log_2(6 - 2x) - \log_2 x = 3$

28. Give the x-intercept of the graph of $y = \log(x - 2)$.

29. Sketch: $x = \sqrt{y}$

30. $\log_{49} \left(\frac{1}{7} \right) =$

31. If $|x - 3| \leq 4$, what is the largest that $|x - 5|$ could possibly be?

32. Find the solution set of $|x + 3| < 7$.

33. Give the domain of: $f(x) = \sqrt{3 - x}$

34. Give the domain of: $f(x) = \frac{3x + 1}{x^2 - 2x}$

35. If $y = f(x)$, describe the transformation of $f(x)$ for $y = 2 + f(-x)$

36. Find the equation of any line perpendicular to $y = 3x + 4$.

37. The equation of a circle whose radius is 4 and whose center is $(1, -3)$ is?

38. The graph of $x - 3y + 12 = 0$ crosses the y-axis at $y = ?$

39. If $f(x) = x^2 - 1$ and $g(x) = 2x + 1$, find $f(g(x))$.

40. Let $f(x) = 2x^{\frac{1}{3}} + 27$. Find $f^{-1}(x)$.

41. Simplify: $(\csc^2 \theta - 1) \tan^2 \theta =$

42. T or F? $\cos^2 x - \sin^2 x = 1$

43. If $\sin A = \frac{-3}{7}$ with A in the third quadrant, find $\cos A$.

45. What is the horizontal distance from the base of a tree 36ft tall if the angle of elevation is 52° ?

47. Which of the following functions is decreasing on its entire domain?

- a) $\cos x$ b) $|x|$
c) $\frac{1}{x}$ d) $10^{\frac{x}{2}}$

49. Which of the following functions Has a "corner" in its graph ?

- a) $f(x) = 7x^2 + 5$ b) $f(x) = |x - 2|$
c) $g(x) = \frac{x+1}{x}$ d) $h(x) = x^3$

51. Find: $\tan(2x)$ if $x = \frac{\pi}{3}$

53. If $px^2 + qx + r = 0$, then $x = ?$

55. If $x > 0, y > 0$, then $\sqrt{27\sqrt{81x^8y^6}} =$

57. Solve the system: $x + 4y = 1$
 $3x + 8y = 2$

59. Simplify: $\frac{6x^4y - 2xy^4}{2xy}$

44. Give the period of: $f(x) = 4\sin(3x)$

46. Simplify: $(\sin x)(\tan x)(\csc^2 x) =$

48. Which of the following is false for Some real number x ?

- a) $x^2 - x + 1 > 0$ b) $x = \sqrt{x^2}$
c) $1 = \frac{x^2 + 1}{x^2 + 1}$ d) $x = \sqrt[3]{x^3}$

50. Which of the following are polynomials?

- a) $x + x^{-1}$ b) $3x^2 + \sqrt{7}x - 8$
c) $\frac{x+1}{x-1}$ d) $\tan(4x)$

52. Find: $\cos(3x)$ if $x = \frac{\pi}{6}$

54. If the length of a rectangle is 8 more than its width, what is the area of the rectangle?

56. If $p(x + q) = qx - s$ and $p \neq q$, then $x = ?$

58. Two cars start moving from the same point. One travels south at 100 km/hr, the other west at 50 km/hr. How far apart are they two hours later?

60. If $f(1) = 3, f(2) = 1, f(3) = 1, g(1) = 2, g(2) = 2$, and $g(3) = 3$. Find: $f(g(f(2) + 2))$.